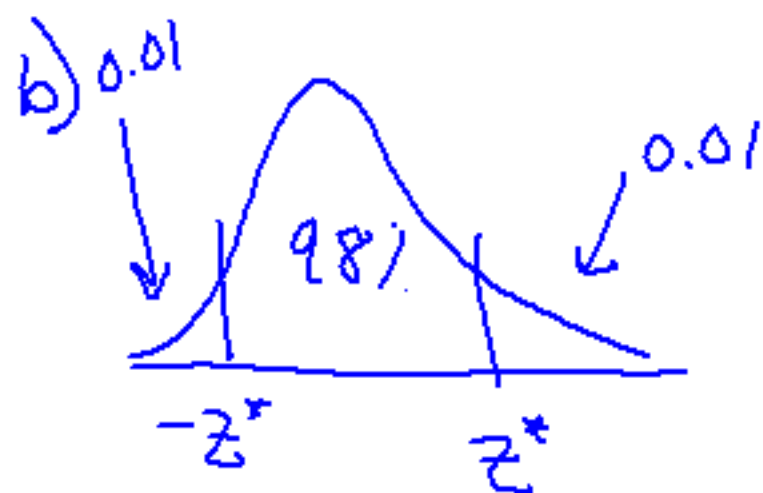


- Get out notes from Friday
- Warm Up: worksheet 6.1- Confidence intervals from notes Friday. Do #3.

$$\textcircled{3} \text{ a) } \bar{x} \pm z^* \cdot \sigma / \sqrt{n} = (4.6298, 6.0102)$$

$$\begin{aligned} \bar{x} &= 5.32 \\ \sigma &= 2.49 \\ n &= 50 \end{aligned}$$

We are 95% conf. that the average drop in heart rate from the drug is btw. 4.6298 and 6.0102 beats/min.



$$\bar{x} \pm z^* \cdot \sigma / \sqrt{n} = (4.5008, 6.1392)$$

\* We are 98% conf. that...

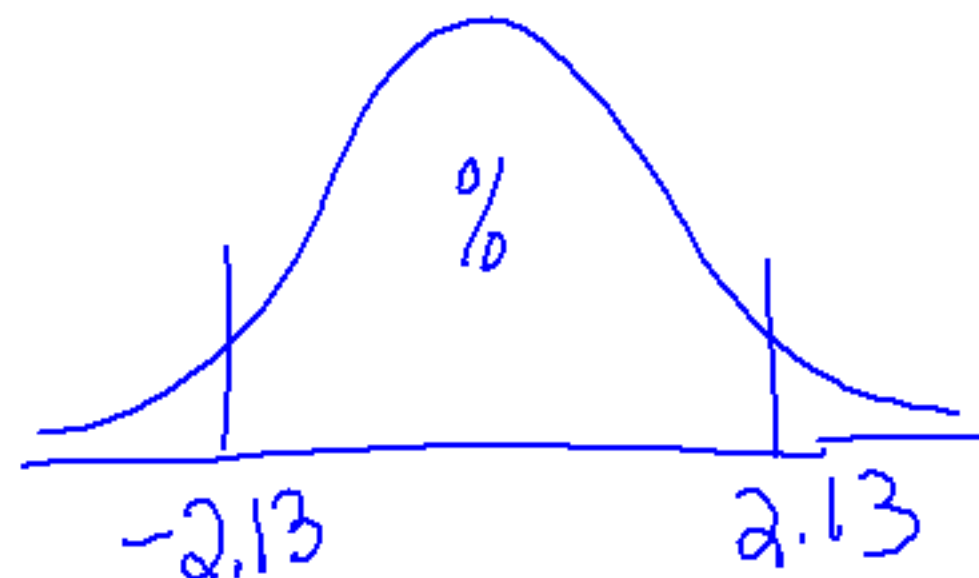
$$\begin{aligned} z^* &= \text{invnorm}(0.01, 0, 1) \\ &= 2.326 \end{aligned}$$

$$\bar{X} \pm \boxed{z^* \cdot \frac{\sigma}{\sqrt{n}}}$$

$$0.75 = z^* \cdot \frac{\sigma}{\sqrt{n}}$$

$$0.75 = z^* \cdot \frac{2.49}{\sqrt{50}}$$

$$z^* = 2.13$$



normcdf(-2.13, 2.13, 0, 1)

96.7%

Assumptions: - must state & check  
for every problem

(u)

STATE

- SRS
- $\sigma$  known
- Normal pop.  
or  
 $n \geq 30$

CHECK

- circled / assumed
- circled
- circled  
or  
 $n = 100 \neq 30$

## Choosing Sample size for a certain m.o.e.

- $\bar{x} \pm z^* \cdot \sigma/\sqrt{n}$
- m.o.e.
- $\uparrow n \Rightarrow \downarrow \text{m.o.e.}$
- so that we have a certain m.o.e.
- $M = z^* \cdot \sigma/\sqrt{n}$       \*round up  $n$
- fill in all vars but  $n$        $n = 102.1 \Rightarrow \textcircled{103}$
- solve for  $n$

Ex

$$m = 2 \text{ lbs.}$$

$$C = 95\%$$

$$n = ?$$

$$\bar{x} = 190.5 \text{ lbs}$$

$$\sigma = 3 \text{ lbs}$$

$$m = z^* \cdot \sigma / \sqrt{n}$$

$$2 = (1.96) \left( \frac{3}{\sqrt{n}} \right)$$

$$n = 8.6436 \Rightarrow \textcircled{9}$$

Wkst  
#1

$$m = z^* \cdot \frac{\sigma}{\sqrt{n}}$$

$$0.01 = \frac{2.576 \cdot 0.025}{\sqrt{n}}$$

$$n = 41.4736 \Rightarrow \textcircled{42}$$

6.2

$$P_{RED} = 0.40$$

R	B

$$\hat{p} = \frac{3}{15} = \underline{0.20}$$

$$\hat{p} = 0.38$$

$$0.35$$

$$0.33$$

$$0.30$$

$$0.25$$

$$P(\hat{p} < 0.20) = \text{normcdf}(-1.9, 0.2, 0.40, \sqrt{\frac{0.4(0.6)}{15}})$$

$$= 0.057$$

- assess the evidence for/against a claim (hypothesis) from sample.
- a sample to a claim (hypothesis)
- expressed in terms of probability.
- Prob. of getting our sample (or something more extreme) if claim is true.



## 5 steps

- a) Assumptions
- b) Hypotheses
- c) Test Statistic
- d) P-value (prob.)
- e) Conclusion



## Hypotheses

- describe the population
- use parameters

### Null Hypothesis

Symbol:  $H_0$

What is it?

~~is~~ claimed to be true  
given

Form:  $H_0: \text{parameter} = \#$   
 $H_0: \mu = \#$

### Alternative Hyp

$H_a$

what you (the researcher)  
believes to be true

$H_a: \text{parameter} \begin{matrix} \geq \\ \neq \end{matrix} \#$   
 $H_a: \mu \begin{matrix} \geq \\ \neq \end{matrix} \#$

same!

If  $H_0$  is still true, then estimate( $\bar{x}$ )  
is close to claim ( $\mu$ )

Alt:

one sided:  $>$ ,  $<$

two-sided:  $\neq$

## Test Stat:

- measure the compatibility btw  $H_0(\mu)$  & your sample ( $\bar{x}$ )
- use test stat. for prob. calc.
- z-score  
Normal R.V.  $N(0,1)$
- $$z = \frac{\bar{X} - \mu}{\sigma/\sqrt{n}}$$

$n =$ 

$z = 1.8$  $z = 2.8$

$z = -0.2$

## P-value

Def: the prob. of getting our sample (or something more extreme) if our claim ( $H_0$ ) is true.

Smaller the p-value...  
the more evidence against  $H_0$ .

P-value:

$$P(Z \geq \overset{\text{sample}}{\text{test statistic}}) = \text{normcdf}(LB, UB, 0, 1)$$

use  $H_a$

Sign. level:

value we say is decisive

$$\alpha = 0.05, 0.01$$

$$p = 0.40$$

$$\hat{p} = 0.38$$

$$0.35$$

$$\rightarrow 0.32$$

$$0.30$$

$$\rightarrow 0.28$$

5%  $\rightarrow$  if I find a sample  
that happens less than  
5% of time, claim is false

$p\text{-value} < \alpha$   
reject  $H_0$